# Mathematics <br> Paper 1 (Non-Calculator) 

## Higher Tier

## Churchill Paper 1A - Marking Guide

> Method marks (M) are awarded for a correct method or partial method
> Process marks (P) are awarded for a correct process as part of a problem solving question
> Accuracy marks (A) are awarded for a correct answer, having used a correct method or process
> (B) marks are unconditional accuracy marks (no method or process needed)
> (C) marks are for communication

# Churchill <br> Maths 

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## Churchill Paper 1A Marking Guide - Edexcel Higher Tier

1 (a) Jeremy marks 1 homework in $60 \div 12=5$ minutes
Kira marks 1 homework in $120 \div 30=4$ minutes
Liz marks 1 homework in 6 minutes
Therefore Kira is the quickest A1
(b) In 20 minutes Jeremy marks 4 homeworks and Kira marks 5 homeworks
Together they mark 9 homeworks in 20 minutes P1
$36 \div 9=4$ so they take $4 \times 20=80$ minutes
$4.30 \mathrm{pm}+80$ minutes $=5.30 \mathrm{pm}+20$ minutes $=5.50 \mathrm{pm}$ A1 They finish marking at 5.50 pm

Total 5

2 (a) 1 chain costs $180 \div 20=£ 9$
1 bead costs $750 \div 500=£ 1.50$
1 spacer costs $90 \div 100=£ 0.90$
1 heart charm costs $120 \div 30=£ 4$

$$
\begin{array}{rlrl}
\text { Total } & =9+(8 \times 1.50)+(4 \times 0.90)+4 & \mathrm{P} 1 \\
& =9+12+3.60+4 & & \text { A1 } \\
& =£ 28.60 &
\end{array}
$$

(b) Profit on 1 bracelet $=39.90-28.60=£ 11.30$

Profit on 15 bracelets $=15 \times 11.30 \quad$ M1

$$
\begin{aligned}
& =10 \times 11.30+5 \times 11.30 \\
& =113+56.50 \\
& =£ 169.50
\end{aligned}
$$

A1 Total 5

3 (a) B and D
(b) $p=4, q=-5$ B2
(c) 2

B1
(d) $x=1$

B1 Total 5
$4 \quad p=4 q-7$
$p+7=4 q \quad$ M1
$q=\frac{p+7}{4}$
A1 Total 2

5 Angle in semi-circle $=90^{\circ}$
$a=180-(90+38)$
M1
$a=180-128$
$a=52$
A1
Total 2

6 (a) (i)

| Number of orders $(N)$ | Cum. Freq. |
| :---: | :---: |
| $40<N \leq 45$ | 4 |
| $40<N \leq 50$ | 21 |
| $40<N \leq 55$ | 54 |
| $40<N \leq 60$ | 79 |
| $40<N \leq 65$ | 99 |
| $40<N \leq 70$ | 113 |
| $40<N \leq 75$ | 120 |

(ii)

B3

(b) 42 (approx, from graph)

Total 6

7 The angles in a triangle add up to $180^{\circ}$ so

$$
\begin{array}{lll} 
& \begin{array}{l}
4 x+3 x+20+5 x-8=180 \\
12 x+12=180 \\
12 x=168 \\
x=14
\end{array} & \text { M1 } \\
& \text { A1 } \\
4 x=56,3 x+20=62 \text { and } 5 x-8=62 & \text { M1 } & \\
\text { As angle } A B C=\text { angle } A C B \text { the triangle is isosceles } \\
\text { The two sides opposite the equal angles are the same length } & & \\
\text { Hence, } A B=A C & \text { C1 } & \text { Total } 4
\end{array}
$$

8 Last week = 100\%
This week $=120 \%=240$
So, $\quad 10 \%=240 \div 12=20$
P1
$100 \%=10 \times 20=200$
A1 Total 2
Leanne sent 200 emails last week

9 (a) $=7 \times 6=42$ ways
B1
(b) Smallest 2 frame sizes:
no. of combinations $=2 \times 7 \times 3=42$ M1
Largest 3 frame sizes:
no. of combinations $=3 \times 7 \times 6=126$
Total no. of combinations $=42+126=168$
A1 Total 3

10 (a) e.g. She can not be sure of this because 10 is a very small number of trials
(b) No. of times red bead picked $=7+6+8+6=27$

No. of trials $=40$
$P($ Faria picks a red bead $)=\frac{27}{40}$
(c) No, she is wrong.

We know the probability that one bead will be green is $\frac{6}{10}$.
However, we don't know the probability that the second will be green, given that the first was green, because we don't know how many beads are in the bag. Her answer assumes that the bag contains 10 beads so that after removing one green bead there are 9 beads left, 5 of which are green.

11 Area of triangular $\mathrm{XS}=\frac{1}{2} \times 9 p \times 2 p=9 p^{2}$
Volume of prism $=9 p^{2} \times 3 p=27 p^{3}$
Let length of edge of cube be $x$
Volume of cube $=x^{3}=27 p^{3}$
$x=\sqrt[3]{27 p^{3}}=\sqrt[3]{27} p=3 p$
P1 A1 Total 3
(a) 8 seconds
(b)


Acceleration $=$ gradient of line $=\frac{12-8}{12-6}=\frac{4}{6}=\frac{2}{3} \mathrm{~m} / \mathrm{s}^{2}$
M1 A1
(c) Distance $=$ area under graph

$$
\begin{array}{ll}
=\left(\frac{1}{2} \times 6 \times 8\right)+\left[\frac{1}{2} \times(8+12) \times 6\right]+(8 \times 12)+\left(\frac{1}{2} \times 16 \times 12\right) & \text { M2 } \\
=24+60+96+96 \\
& 276 \mathrm{~m}
\end{array}
$$

Total 6
$135 y=\left(4 \times 10^{7}\right)+\left(2 \times 10^{6}\right)$
$5 y=\left(4 \times 10^{7}\right)+\left(0.2 \times 10^{7}\right)$
$5 y=4.2 \times 10^{7}$
$10 y=8.4 \times 10^{7}$
$y=8.4 \times 10^{6}$
P1 A1 Total 3

14 In a normal week, let Henrik earn $h$ and Rob earn $r$
$h: r=3: 2$ so $h=\frac{3}{2} r$
B1
$h+20: r+20=4: 3$ so $h+20=\frac{4}{3}(r+20)$

$$
\begin{equation*}
3(h+20)=4(r+20) \tag{P1}
\end{equation*}
$$

$$
\begin{equation*}
3 h+60=4 r+80 \tag{2}
\end{equation*}
$$

Sub (1) into (2)

$$
\begin{equation*}
3 \times \frac{3}{2} r+60=4 r+80 \tag{P1}
\end{equation*}
$$

$\frac{9}{2} r+60=4 r+80$
$\frac{1}{2} r=20$

$$
r=40
$$

So, $h=\frac{3}{2} \times 40=60$
In the week before Christmas, Henrik earns $h+20=£ 80$
A1 Total 4

15 (a)

| $\sin 0^{\circ}$ | $\sin 30^{\circ}$ | $\sin 45^{\circ}$ | $\sin 60^{\circ}$ | $\sin 90^{\circ}$ |
| :---: | :---: | :---: | :---: | :---: |
| 0 | $\frac{1}{2}$ | $\frac{\sqrt{2}}{2}$ | $\frac{\sqrt{3}}{2}$ | 1 |

(b) Area $A B C=\frac{1}{2} \times 6 \times 8 \times \sin 30^{\circ}$

$$
\begin{aligned}
& =24 \times \frac{1}{2} \\
& =12 \mathrm{~cm}^{2} \\
\text { Area } P Q R & =\frac{1}{2} \times 3 \times 8 \times \sin 45^{\circ} \\
& =12 \times \frac{\sqrt{2}}{2} \\
& =6 \sqrt{2} \mathrm{~cm}^{2}
\end{aligned}
$$

Triangle $A B C$ has the larger area

16 (a) $g(5)=\frac{5+3}{2}=4$
$\mathrm{fg}(5)=\mathrm{f}(4)=3 \times 4-1=11$ A1
(b) Let $\mathrm{g}(x)=-2$

$$
\begin{aligned}
& \frac{x+3}{2}=-2 \\
& x+3=-4 \\
& x=-7 \\
& \text { Therefore } \mathrm{g}^{-1}(-2)=-7
\end{aligned}
$$

$$
\text { A1 } \quad \text { Total } 4
$$

17 David is not correct
e.g. When $x=\frac{1}{16}: \quad \sqrt{x}=\sqrt{\frac{1}{16}}=\frac{1}{4}$

$$
\sqrt[4]{x}=\sqrt[4]{\frac{1}{16}}=\frac{1}{2}
$$

$\frac{1}{4}<\frac{1}{2}$ making his statement incorrect
[Any value in the interval $0<x<1$ can be used]

18 Sub $P(2 a, a)$ into equation: $(2 a)^{2}+a^{2}=80$

$$
\begin{equation*}
5 a^{2}=80 \tag{P1}
\end{equation*}
$$

$$
a^{2}=16
$$

$$
a=4 \quad \text { [can't be }-4 \text { as positive constant] }
$$

$P$ is $(8,4)$
Gradient of $O P=\frac{4-0}{8-0}=\frac{1}{2}$
Gradient of tangent $=\frac{-1}{\left|\frac{1}{2}\right|}=-2$
Equation of tangent: $\quad y=-2 x+c$

$$
\begin{align*}
& 4=(-2 \times 8)+c  \tag{P1}\\
& c=4+16=20
\end{align*}
$$

Hence,
$y=-2 x+20$
$y$-intercept $=20$ so $R$ is $(0,20)$
Crosses $x$-axis when $y=0$ :

$$
\begin{aligned}
& 0=-2 x+20 \\
& 2 x=20 \\
& x=10 \text { so } Q \text { is }(10,0)
\end{aligned}
$$

Area of $O Q R=\frac{1}{2} \times 10 \times 20=100$

19 (a) $\overrightarrow{X Y}=\overrightarrow{X O}+\overrightarrow{O Y}$

$$
\begin{align*}
& =-\frac{1}{2} \overrightarrow{O A}+\frac{1}{3} \overrightarrow{O C}  \tag{P1}\\
& =-2 p+2 q \tag{A1}
\end{align*}
$$

(b) $\overrightarrow{B C}=\overrightarrow{B O}+\overrightarrow{O C}$

$$
\begin{align*}
& =-\overrightarrow{O B}+\overrightarrow{O C} \\
& =-(3 \mathbf{p}+3 \mathbf{C})+6 \mathbf{q}  \tag{P1}\\
& =-3 \mathbf{p}+3 \mathbf{q} \\
& =\frac{3}{2} \overrightarrow{X Y}
\end{align*}
$$

As $\overrightarrow{B C}$ is a multiple of $\overrightarrow{X Y}$ they have the same direction so $B C$ is parallel to $X Y$

A1 Total 4

20 (a) (i) $x^{2}+4 x-3=(x+2)^{2}-2^{2}-3$
P1
$=(x+2)^{2}-7$
A1
(ii) $\quad(x+2)^{2}-7=0$

$$
\begin{align*}
& (x+2)^{2}=7 \\
& x+2= \pm \sqrt{7} \\
& x=-2 \pm \sqrt{7} \tag{B1}
\end{align*}
$$

(b) $y=1 \pm \sqrt{2}$
$y-1= \pm \sqrt{2}$
$(y-1)^{2}=2$
P1
$y^{2}-2 y+1=2$
P1
$y^{2}-2 y-1=0$
$a=-2$ and $b=-1$
A1 Total 6

